

Teaching Notes for Algebra I

Homework #6

Overview: In this lesson, students will learn how to apply algebra concepts to basic geometry concepts and will use their translate and simply skills to solve word problems.

Preparation: Watch videos on “math god” and “translate and simplify.”

Classroom Examples:

- 1) Complimentary angles where one is $3x + 7$ and the other is $4x - 8$.

$$\begin{array}{rcl} (3x + 7) + (4x - 8) = 90 & 3x + 7 & 4x - 8 \\ 7x - 1 = 90 & 3(13) + 7 & 4(13) - 8 \\ 7x = 91 & 39 + 7 & 52 - 8 \\ x = 13 & 46 & 44 \end{array}$$

- 2) Supplementary angles where one is $5x - 3$ and the other is $2x + 8$.

$$\begin{array}{rcl} (5x - 3) + (2x + 8) = 180 & 5x - 3 & 2x + 8 \\ 7x + 5 = 180 & 5(25) - 3 & 2(25) + 8 \\ 7x = 175 & 125 - 3 & 50 + 8 \\ x = 25 & 122 & 58 \end{array}$$

- 3) Vertical angles where one is $7x - 9$ and the other is $3x + 7$.

$$\begin{array}{rcl} 7x - 9 = 3x + 7 & 7x - 9 & 3x + 7 \\ 4x - 9 = 7 & 7(4) - 9 & 3(4) + 7 \\ 4x = 16 & 28 - 9 & 12 + 7 \\ x = 4 & 19 & 19 \end{array}$$

- 4) Five full circle angles where each one is $3x + 2$, $4x$, $5x - 6$, $x + 5$, and, $2x - 1$.

$$\begin{array}{l} (3x + 2) + (4x) + (5x - 6) + (x + 5) + (2x - 1) = 360 \\ 15x = 360 \\ x = 24 \end{array}$$

$$\begin{array}{rcccl} 3x + 2 & & 5x - 6 & & 2x - 1 \\ 3(24) + 2 & 4x & 5(24) - 6 & x + 5 & 2(24) - 1 \\ 72 + 2 & 4(24) & 120 - 6 & 24 + 5 & 48 - 1 \\ 74 & 96 & 114 & 29 & 47 \end{array}$$

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- 5) Five more than triple the difference of a number and four is seven less than the number.

$$3(x-4)+5=x-7$$

$$3x-12+5=x-7$$

$$3x-8=x-7$$

$$2x-8=-7$$

$$2x=1$$

$$x=\frac{1}{2}$$

- 6) Eight less than the quotient of a number and four is nine more than twice the number.

$$\frac{x}{4}-8=2x+9$$

$$-8=\frac{9x}{4}+9$$

$$-17=\frac{9x}{4}$$

$$68=9x$$

$$\frac{68}{9}=x$$

- 7) If twice the sum of three consecutive integers is 312, find the three integers.

1st	2nd	3rd
x	$x+1$	$x+2$

$$2(x+(x+1)+(x+2))=312$$

$$2(x+x+1+x+2)=312$$

$$2(3x+3)=312$$

$$6x+6=312$$

$$6x=318$$

$$x=53$$

53,54,55

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- 8) If seven less than triple the sum of the first and third of three consecutive even integers is thirty-seven more than five times the middle integer, find the three integers.

$$\begin{array}{ccc} \text{1st} & \text{2nd} & \text{3rd} \\ x & x+2 & x+4 \end{array}$$

$$3(x + (x + 4)) - 7 = 5(x + 2) + 37$$

$$3(x + x + 4) - 7 = 5(x + 2) + 37$$

$$3(2x + 4) - 7 = 5(x + 2) + 37$$

$$6x + 12 - 7 = 5x + 10 + 37$$

$$6x + 5 = 5x + 47$$

$$x + 5 = 47$$

$$x = 42$$

42, 44, 46

- 9) If three less than double the sum of three consecutive odd integers is two hundred nineteen, find the three integers.

$$\begin{array}{ccc} \text{1st} & \text{2nd} & \text{3rd} \\ x & x+2 & x+4 \end{array}$$

$$2(x + (x + 2) + (x + 4)) - 3 = 219$$

$$2(x + x + 2 + x + 4) - 3 = 219$$

$$2(3x + 6) - 3 = 219$$

$$6x + 12 - 3 = 219$$

$$6x + 9 = 219$$

$$6x = 210$$

$$x = 35$$

35, 37, 39

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- 10) The sum of two numbers is 42. If five more than triple the smaller is nine less than twice the larger, find the two numbers.

Large Small

$$x \quad 42 - x$$

$$3(42 - x) + 5 = 2(x) - 9$$

$$126 - 3x + 5 = 2x - 9$$

$$131 - 3x = 2x - 9$$

$$131 = 5x - 9$$

$$140 = 5x$$

$$28 = x$$

28,14

- 11) The difference of two numbers is seven. If two less than the sum of the two numbers is one more than triple the smaller, find the two numbers.

Large Small

$$x \quad x - 7$$

$$(x + (x - 7)) - 2 = 3(x - 7) + 1$$

$$x + x - 7 - 2 = 3x - 21 + 1$$

$$2x - 9 = 3x - 20$$

$$-9 = x - 20$$

$$11 = x$$

11,4