

Pre-Calculus Homework #15 – Answer Key

1)

$$\csc x - \cos x \cot x = \sin x$$

$$\frac{1}{\sin x} - \cos x \cdot \frac{\cos x}{\sin x} = \sin x$$

$$\frac{1 - \cos^2 x}{\sin x} = \sin x$$

$$\frac{\sin^2 x}{\sin x} = \sin x$$

$$\sin x = \sin x$$

2)

$$(\sin \theta + \cos \theta)^2 = 1 + \sin 2\theta$$

$$\sin^2 \theta + 2 \sin \theta \cos \theta + \cos^2 \theta = 1 + \sin 2\theta$$

$$1 + 2 \sin \theta \cos \theta = 1 + \sin 2\theta$$

$$1 + \sin 2\theta = 1 + \sin 2\theta$$

3)

$$(\csc \alpha + \cot \alpha)^2 = \frac{1 + \cos \alpha}{1 - \cos \alpha}$$

$$\left(\frac{1}{\sin \alpha} + \frac{\cos \alpha}{\sin \alpha}\right)^2 = \frac{1 + \cos \alpha}{1 - \cos \alpha} \cdot \frac{1 + \cos \alpha}{1 + \cos \alpha}$$

$$\left(\frac{1 + \cos \alpha}{\sin \alpha}\right)^2 = \frac{(1 + \cos \alpha)^2}{1 - \cos^2 \alpha}$$

$$\frac{(1 + \cos \alpha)^2}{\sin^2 \alpha} = \frac{(1 + \cos \alpha)^2}{\sin^2 \alpha}$$

4)

$$\frac{1 + \sin \beta}{1 + \csc \beta} = \frac{\tan \beta}{\sec \beta}$$

$$\frac{\sin \beta}{\cos \beta}$$

$$\frac{1 + \sin \beta}{1 + \frac{1}{\sin \beta}} = \frac{\sin \beta}{\cos \beta}$$

$$\frac{1 + \sin \beta}{\frac{\sin \beta + 1}{\sin \beta}} = \frac{\sin \beta}{\cos \beta}$$

$$\frac{1 + \sin \beta}{\sin \beta + 1} = \frac{\sin \beta}{\cos \beta} \cdot \frac{\cos \beta}{1}$$

$$\sin \beta$$

$$\frac{1 + \sin \beta}{1} \cdot \frac{\sin \beta}{\sin \beta + 1} = \sin \beta$$

$$\sin \beta = \sin \beta$$

5)

$$\frac{\tan y + \sin y}{2 \tan y} = \cos^2\left(\frac{y}{2}\right)$$

$$\frac{\frac{\sin y}{\cos y} + \frac{\sin y}{1}}{\frac{2 \sin y}{\cos y}} = \frac{1 + \cos y}{2}$$

$$\frac{\sin y + \sin y \cos y}{\cos y} \cdot \frac{\cos y}{2 \sin y} = \frac{1 + \cos y}{2}$$

$$\frac{\sin y(1 + \cos y)}{\cos y} \cdot \frac{\cos y}{2 \sin y} = \frac{1 + \cos y}{2}$$

$$\frac{1 + \cos y}{2} = \frac{1 + \cos y}{2}$$

6) $\theta = 30^\circ, 150^\circ, 210^\circ, 330^\circ$

7) $\frac{\sqrt{6} + \sqrt{2}}{4}$ or $\frac{\sqrt{2 + \sqrt{3}}}{2}$

8) $\theta = 0, \frac{2\pi}{3}, \pi, \frac{4\pi}{3}$

9) $-2 - \sqrt{3}$ or $-\sqrt{7 + 4\sqrt{3}}$

10) $\theta = 0^\circ, 90^\circ, 180^\circ, 270^\circ$

11) $\frac{\sqrt{\sqrt{2} + 2}}{2}$

12) $\theta = 0, \frac{\pi}{2}, \pi, \frac{3\pi}{2}$

13) $2 + \sqrt{3}$ or $\sqrt{7 + 4\sqrt{3}}$

14) $\theta = 135^\circ, 315^\circ$

15) $\frac{-\sqrt{2 - \sqrt{2}}}{2}$

16) $\theta = \frac{\pi}{6}, \frac{\pi}{2}, \frac{5\pi}{6}, \frac{7\pi}{6}, \frac{3\pi}{2}, \frac{11\pi}{6}$

17) $\sin 2\theta = \frac{24}{25}$ $\cos 2\theta = \frac{-7}{25}$ $\tan 2\theta = \frac{-24}{7}$ quadrant II

18) $\theta = 63.435^\circ, 104.036^\circ, 243.435^\circ, 284.036^\circ$

19) $\sin 2\theta = \frac{-240}{289}$ $\cos 2\theta = \frac{-161}{289}$ $\tan 2\theta = \frac{240}{161}$ quadrant III

20) $\theta = 1.571, 4.261, 5.163$